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# Protein amyloid self assembly: nucleation, growth, and breakage

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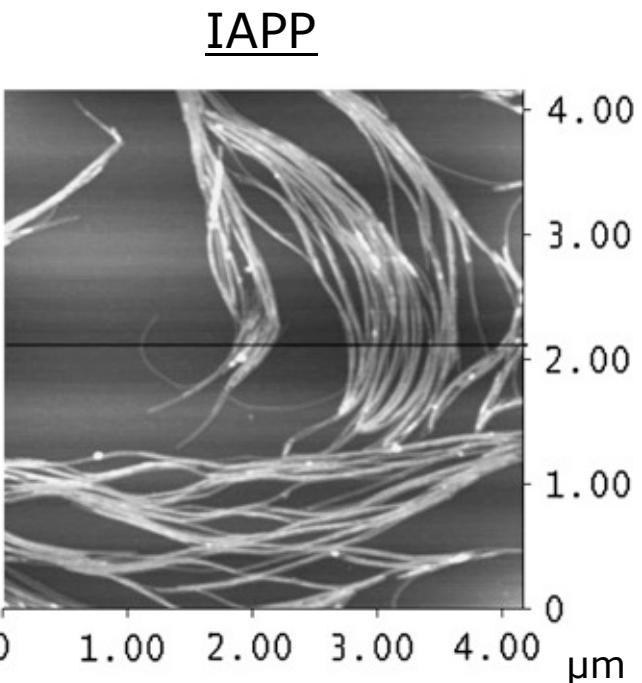
# Protein amyloids

Amyloid fibrils are linear aggregates of proteins

Many proteins form amyloids

Many amyloid related diseases, e.g., Alzheimer's, Parkinson, Type II diabetes

Amyloid fibrils form easily *in vitro*



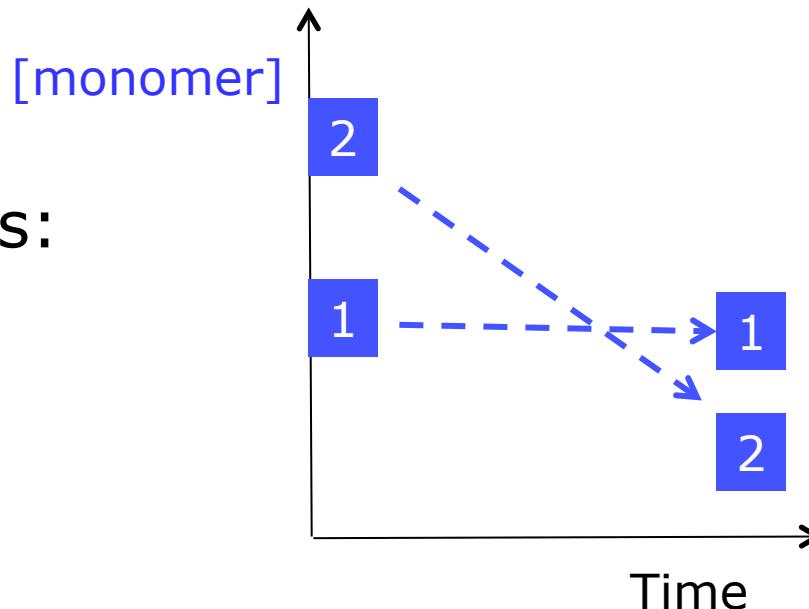
Lopes et al. (2007) *Biophys. J*

# Plan

- Nucleation of amyloid fibrils
- Dynamics of fibril elongation
- Thermal breakage

# A Paradox

In vitro observations:  
2 experiments



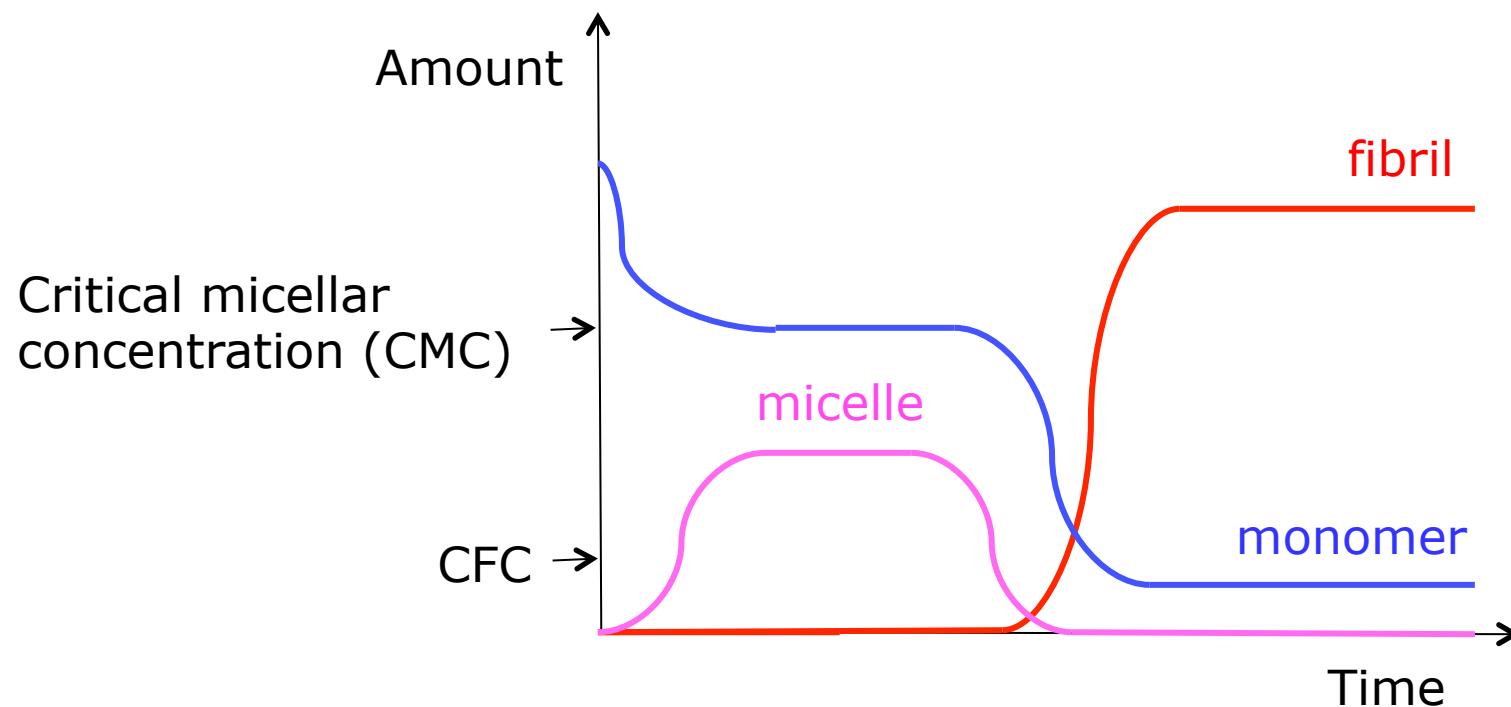
Expt 1: Medium [monomer]  $\rightarrow$  medium [monomer]  
Expt 2: High [monomer]  $\rightarrow$  low [monomer]

→ Nucleation pathway: monomer  $\rightarrow$  micelle  $\rightarrow$  nucleus (fibril)

Lomakin, Teplow, Kirschner and Benedek (1997) *PNAS* **94**, 7942

# A second critical conc.

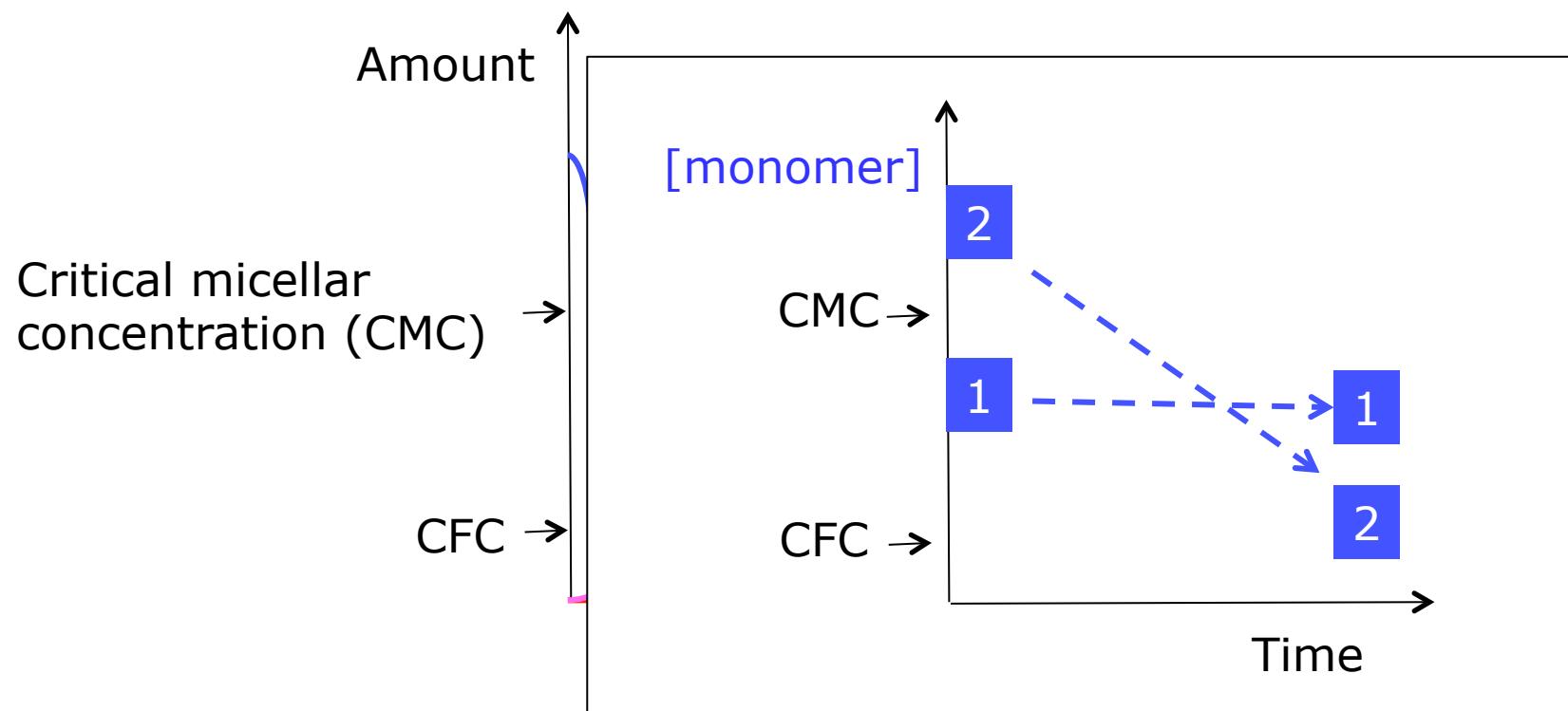
Observable pathway: monomer  $\rightarrow$  micelle  $\rightarrow$  nucleus (fibril)



Lomakin, Teplow, Kirschner and Benedek (1997) *PNAS* **94**, 7942  
Lee (2009) *PRE* **80**, 031922

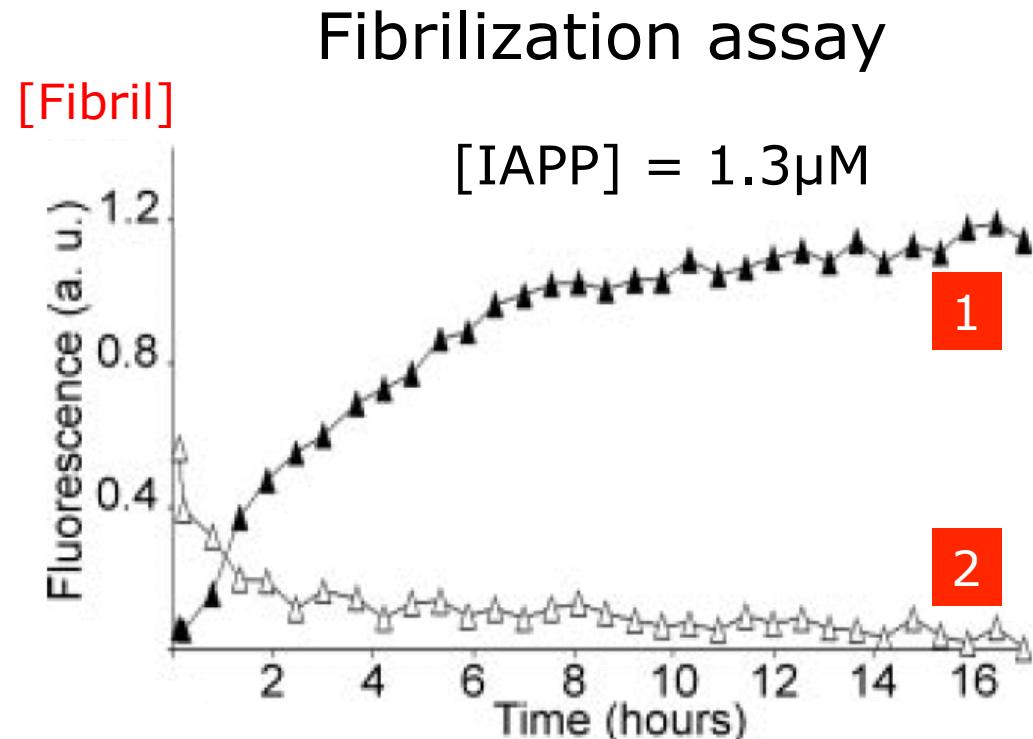
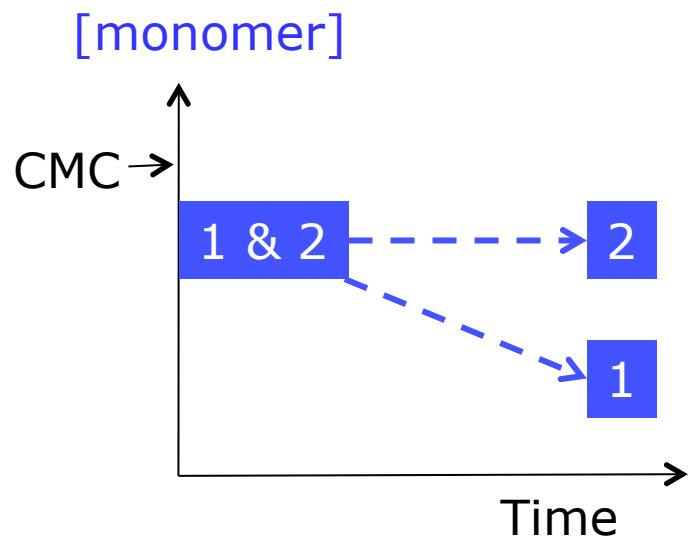
# A second critical conc.

Observable pathway: monomer  $\rightarrow$  micelle  $\rightarrow$  nucleus (fibril)



Lomakin, Teplow, Kirschner and Benedek (1997) *PNAS* **94**, 7942  
Lee (2009) *PRE* **80**, 031922

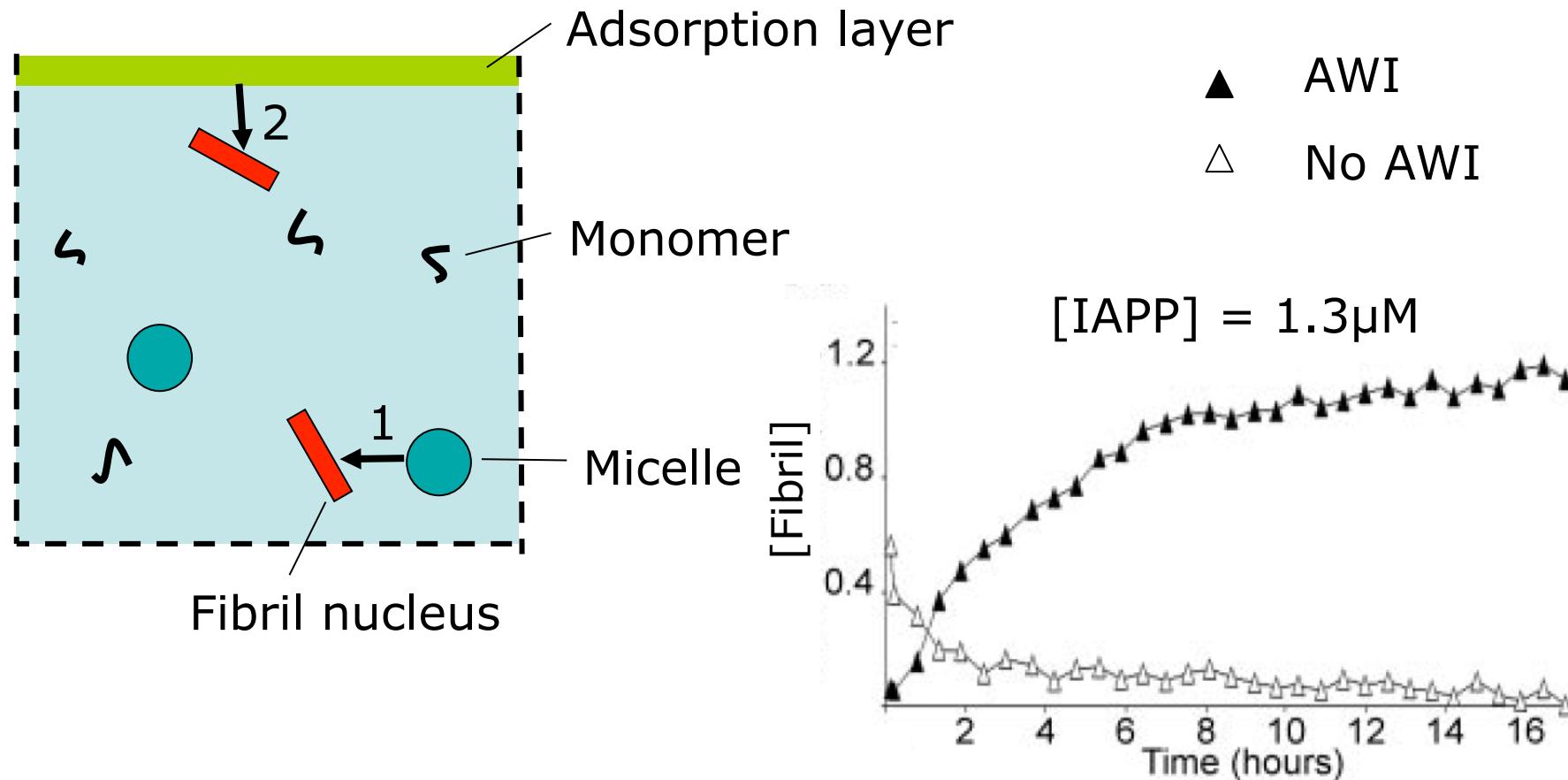
# Interfacial effect



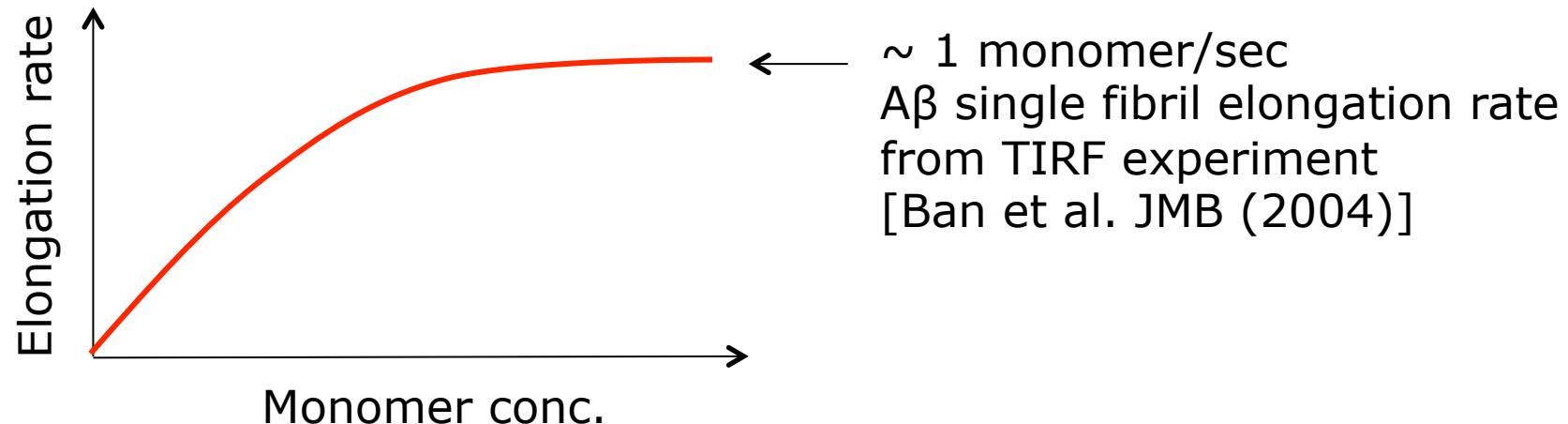
Expt 1: with Air-Water Interface (AWI),  $\blacktriangle$   
Expt 2: no AWI,  $\triangle$

Jean, Lee, Lee, Shaw and Vaux (2010) *FASEB Journal* **24**, 309

# Two fibrilization pathways



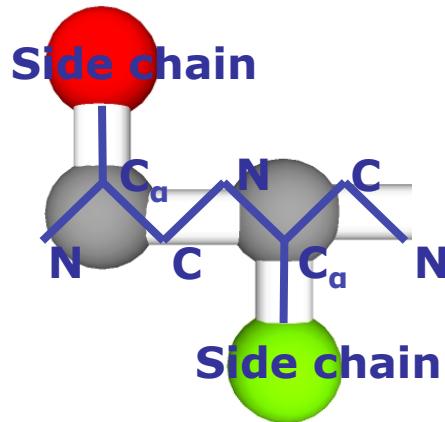
# Fibril Elongation



## Question:

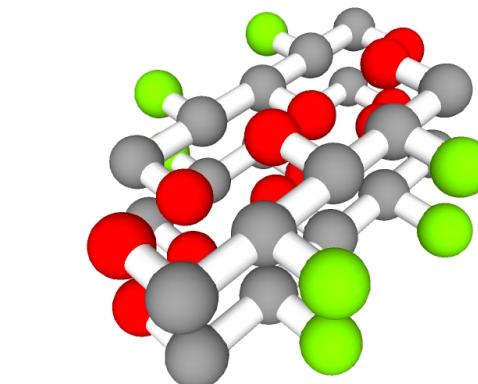
Can we explain the time scale observed?

# Coarse-grained molecular dynamics simulations

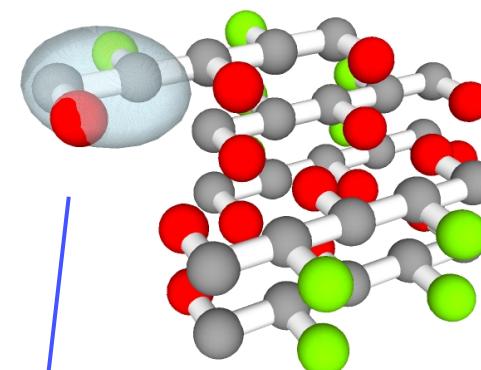


Diffusion in rugged  
energy landscape  
[Zwanzig, PNAS ('88)]

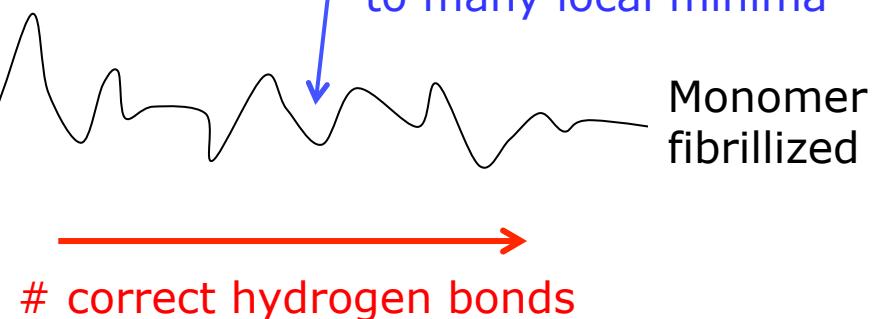
$$D_{eff} = D \exp \left[ - \left( \frac{\Delta E}{k_B T} \right)^2 \right]$$



Separate  
monomer  
& fibril



Misalignment leads  
to many local minima



Lee, Loken, Jean and Vaux (2009) Physical Review E 80, 041906

# Thermal Breakage

M beads connected by springs in 1D

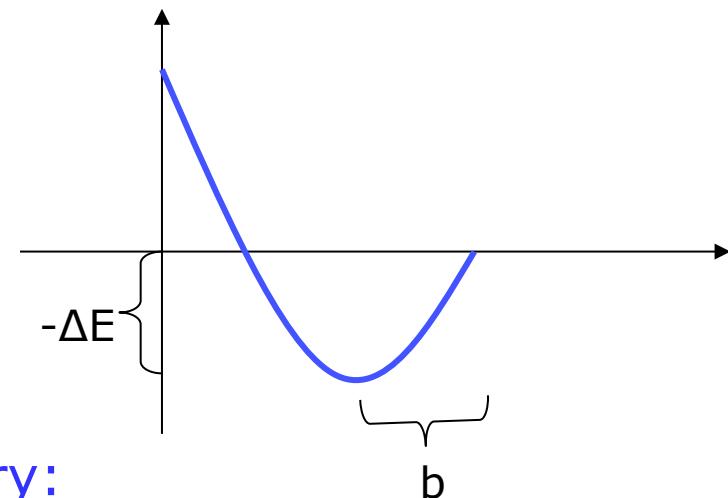


$$\zeta \frac{dx}{dt} = f(x) + \sqrt{2\zeta k_B T} g(t)$$

Friction coefficient

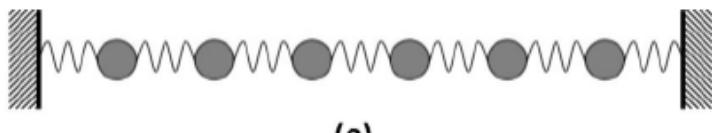
Multidimensional Kramers escape theory:

$$\text{Breakage rate: } R = \frac{8\Delta E^{3/2} M}{b^2 \zeta \sqrt{\pi k_B T}} \exp[-\Delta E / k_B T]$$

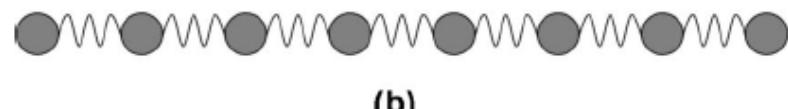


Lee (2009) Phys. Rev. E 80, 031134

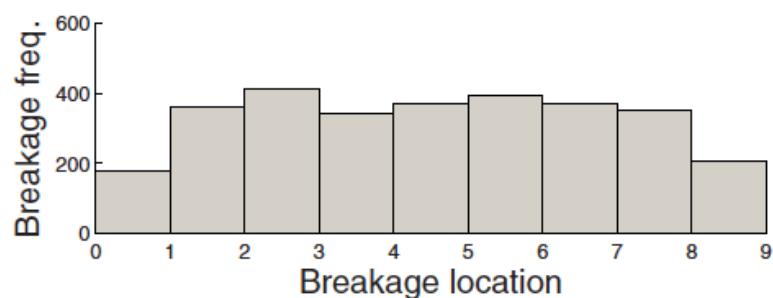
# Breakage Profile



(a)



(b)



Lee (2009) Phys. Rev. E 80, 031134

# Summary

- Protein amyloids are physiologically and technologically important
- Heterogeneous nucleation
  - Interface dominated at low concentration
- Slow dynamics of fibril elongation
  - Diffusion in a rugged energy landscape due to misalignment
- Thermal breakage
  - Multidimensional Kramers problem
  - Uniform breakage propensity for free fibrils
  - Tethered points break half as often

# Thanks

Oxford's Dunn School of Pathology (experiments)

Catherine Davison  
Chongsoo Lee  
Michael Shaw

Oxford's Particle Physics Sub-Department  
(grid computation infrastructure)

James Loken  
Rhys Newman  
Jeff Tseng

# Thank you!

## References

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- C.F. Lee (2009) Self-assembly of protein amyloid: A competition between amorphous and ordered aggregation. *Physical Review E* 80, 031922
- C.F. Lee, J. Loken, L. Jean and D.J. Vaux (2009) Elongation dynamics of amyloid fibrils: a rugged energy landscape picture. *Physical Review E* 80, 041906
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